Analysis of electric power and energy systems

Lecture 4: Transformers, power flow analysis part 2

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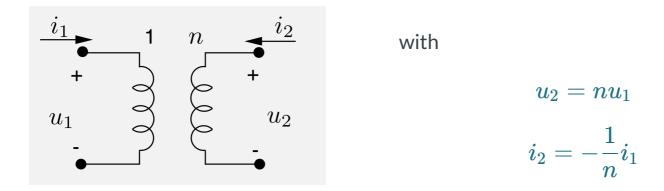
What will we learn today?

- The power transformer
- The next part of power flow analysis: how to include transformers and transformers with tap changers

You will be able to do exercises 6.2, 6.3, 6.4 from Ned Mohan's book.

The transformer

A (single phase) transformer is made of two magnetically coupled coils or windings. An ideal transformer is a two-port represented as



In power systems, transformers are mainly used to transmit power over long distances by changing the voltage level, thus decreasing the current for a given power level. The voltage level of a synchronous generator is around 20kV.

Voltage is changed around five times between generation and load.

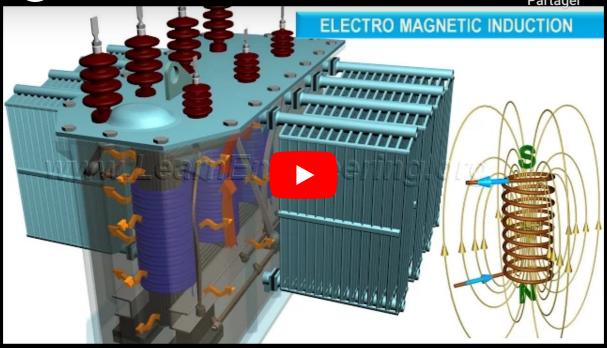
It is also used to measure currents and voltages, electrically isolate parts of a circuit (not the auto-transformer we will see), and match impedances.



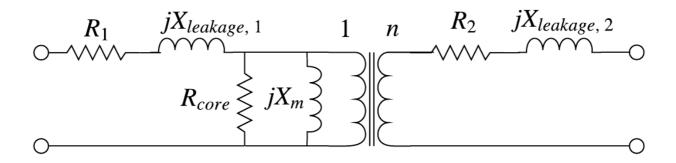
How does a Transformer work?







Non-ideal model



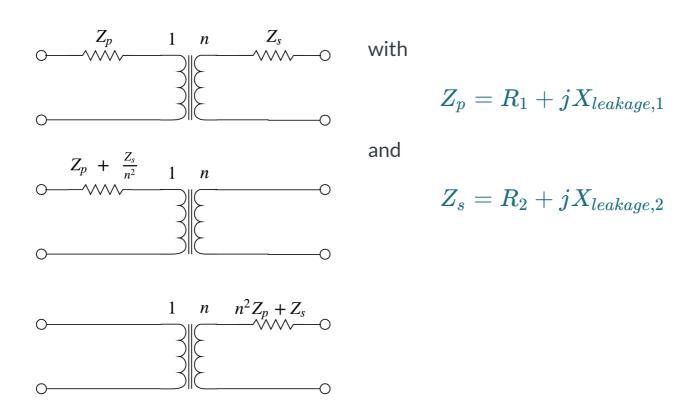
The ideal model is complemented by elements

- ullet X_m that models the magnetizing inductance
- ullet $X_{leakage,i}$ that models the flux not captured by the core on side i
- ullet R_{core} that models eddy current and hysteresis losses, i.e., losses in the iron core
- R_1 and R_2 that model (coil) copper losses

Parameters are either given in the datasheet or obtained by open-circuit and short-circuit tests.

Laminated core to decrease losses.

The excitation current, the sum of the currents in R_{core} and X_m , is often neglected, leading to a simpler non-ideal model, and the series impedances can be transferred from one side to the other:



Per unit representation

Let's consider the rated voltages and currents on both sides of the (ideal) transformer as base values. As

$$V_{s,base} = nV_{p,base}$$

and

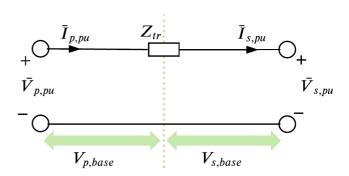
$$I_{p,base} = nI_{s,base},$$

the MVA base is the same on both sides, and thus

$$Z_{s,base} = n^2 Z_{p,base}$$

Hence, in per unit, the transformer can be replaced by a single impedance

$$Z_{tr} = rac{Z_p}{Z_{p,base}} + rac{Z_s}{Z_{s,base}}.$$



Thus we have also that

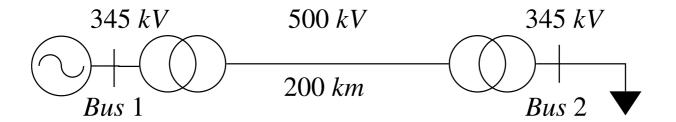
$$egin{aligned} Z_{tr} &= rac{Z_p + Z_s/n^2}{Z_{p,base}} \ &= rac{n^2 Z_p + Z_s}{Z_{s,base}} \end{aligned}$$

i.e. the impedance is the same whether we see it from the primary or the secondary side, although the voltage bases differ.

Also, if the three-phase transformer is wye-delta connected, a 30° phase shift must be applied (more on this later).

Example 6.1

Consider the one-line diagram



with

- ullet a 200 km line with $R=0.029\Omega/km, X=0.326\Omega/km$, neglected shunt impedances
- two transformers with a leakage reactance of 0.2pu in the (500 kV, 1000 MVA) base, and losses neglected.

What is the equivalent model in a (345 kV, 100 MVA) base?

In the (500 kV, 1000 MVA) base:

 $Z_{line,pu} = 200 imes (0.029 + j0.326)/(500^2/1000) = 0.0232 + j0.2608pu$

• hence, the total impedance between buses 1 and 2 is

$$Z_{12} = 0.0232 + j0.2608 + 2 * j0.2pu = 0.0232 + j0.6608pu$$

In the (345 kV, 100 MVA) base:

- the pu value of the impedance is the same in the (500 kV, 1000 MVA) and (345 kV, 1000 MVA) bases,
 - since we can transfer the impedance from one side of each transformer to the other, cf. a previous remark
- if we now change the MVA base to 100 MVA,

$$Z_{12} = (0.0232 + j0.6608) imes (100/1000) pu = 0.00232 + j0.06608 pu$$

since the base impedance is proportional to the inverse of the MVA base.

Efficiency

The efficiency expressed in % is

$$100 imes rac{P_{output}}{P_{input}} = 100 imes \left(1 - rac{P_{losses}}{P_{input}}
ight)$$

- maximal when loaded such that copper losses = iron losses (cancel derivative of efficiency w.r.t current)
- Around 99.5 % in large power transformers at full load.

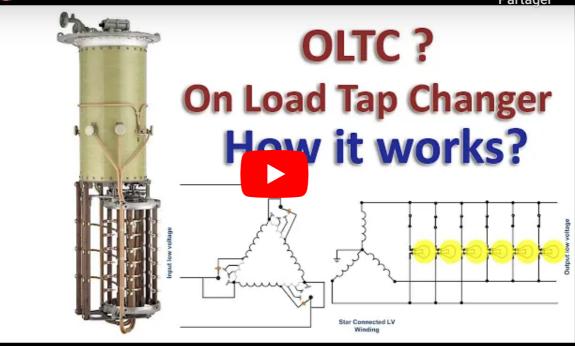
Tap changers

- ullet Some transformers are equipped with a system allowing to change the 1:n ratio
- The ability to change the tap under load is called load tap changer (LTC) or onload tap changer (OLTC)
- This is mainly used for voltage control
- It is usually implemented using auto-transformers
- We will see later on how to include this in the power flow analysis



On Load Tap Changer :- How it works?





Auto-transformers

The two windings (of the same phase) are connected in series, without galvanic insulation. They are commonly used when the ratio is limited.

Advantages:

- Physically smaller
- less costly (less copper)
- higher efficiency
- easy to implement tap changes
- "solid" earth grounding

Disadvantages:

- no electrical insulation
- higher short circuit current
- full voltage at secondary if it breaks (in case of a step down)



Auto Transformer working principle, how Variac works, ...



Partager

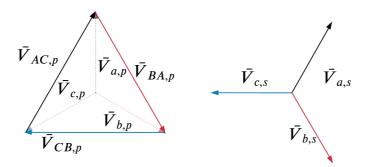


Phase shift in delta-star transformers

The star part has n times the number of turns of the delta part (primary side).

Let's reason on phase a,

- Voltage $\bar{V}_{a,s}$ is on the same core as $\bar{V}_{AC,p}=\sqrt{3}\bar{V}_{a,p}\angle-30^\circ$ where $\bar{V}_{a,p}$ is the (virtual) phase-neutral voltage on the primary side.
- Since $ar{V}_{a,s}=nar{V}_{AC,p}$, $ar{V}_{a,s}=n\sqrt{3}ar{V}_{a,p}\angle-30^\circ$



We gain a $\sqrt{3}$ factor in the amplification, but a lagging phase shift of 30°.

The same reasoning holds for phases b and c.

Power flow regulation by phase shifting

We have seen in lecture 2 that active power flows are dictated by the voltage magnitudes but also the sine of the angle difference between buses:

$$\overline{V}_s \stackrel{\stackrel{\bullet}{\longleftarrow}}{\stackrel{\bullet}{\longleftarrow}} \overline{V}_r = V_r$$

$$S_r = ar{V}_r ar{I}^* = V_r \left(rac{V_s \angle - \delta - V_r}{-j X}
ight)$$
 $\overline{V}_r = V_r \qquad = rac{V_s V_r \sin \delta}{X} + j rac{V_s V_r \cos \delta - V_r^2}{X}$

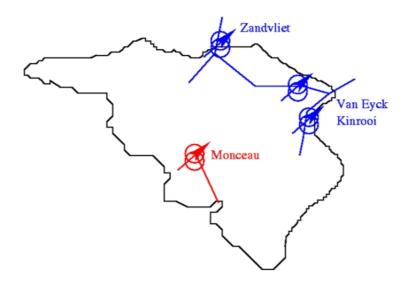
 δ is the angle between V_r and V_s

If we have a device that can generate an adjustable phase shift, we can control the power flows. This is the purpose of phase-shifting transformers.

In practice phase shifting is achieved by "combining the signal with a fraction of itself shifted by 90°". For the details of how it is implemented or modeled, see

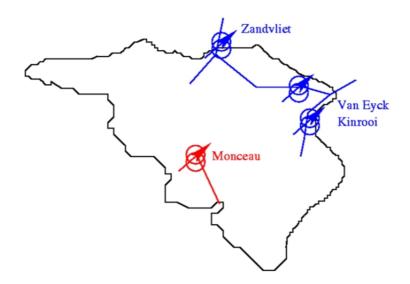
- Wikipedia
- Section 5.7. of the Weedy or ELEC0014.
- ENTSO-E Phase Shift Transformers Modelling, Version 1.0.0, May 2015

Example: phase shifting transformers on the borders of Belgium



380/380 kV: in series with:

- 1. line Zandvliet (B) Borssele (NL) and Zandvliet (B) Geertruidenberg (NL)
- 2. line Meerhout (B) Maasbracht (NL)
- 3. line Gramme (B) Maasbracht (NL)
 - nominal power 3VN Imax = 1400 MVA
 - ∘ phase shift adjustment: 35 positions, +17/-17 × 1.5° (at no load)



220/150 kV:

• in series with the Chooz (F) - Monceau (B) line nominal power: 400 MVA

• in-phase adjustment: 21 positions, +10/-10 × 1.5 %

• quadrature adjustment: 21 positions, +10/-10 × 1.2°

Remarks

In three-phase operation,

- either there are three separate single-phase transformers (easier to fix when there is a problem on a phase, more modular)
- or a three-phase transformer, that is a single core with three autotransformers on it, cf. the video at the beginning of this presentation (cheaper, lighter core and less copper).

Some transformers called three-winding transformers are equipped with a third winding (not to be confused with a three-phase transformer) that is used for auxiliary purposes (feeding auxiliary devices e.g., fans, providing reactive power support, ...).

Transformers in the power flow analysis

Transformer without regulation

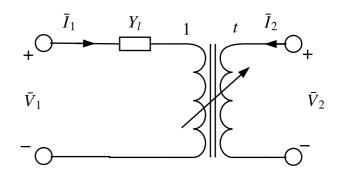
A transformer, in the per-unit representation, can thus be represented

- as a two-port if the shunt admittance is considered
- as a simple series leakage impedance if the shunt admittance is neglected

Representing taps and phase shifts

Let Y_l be the leakage admittance and t be the off-nominal turns ratio:

- ullet if $0 < t \leq 1$, this corresponds to a simple tap-changer
- if $0<|t|\le 1$ but is complex, then this is a phase-shifter ($\angle t<\pi/2$)



We have

$$ar{I}_1 = \left(ar{V}_1 - rac{ar{V}_2}{t}
ight)Y_l$$

and since $rac{ar{V}_2}{t}ar{I}_1^\star = -ar{V}_2ar{I}_2^\star$ by energy conservation

$$ar{I}_2 = -rac{ar{I}_1}{t^\star} = -ar{V}_1rac{Y_l}{t^\star} + ar{V}_2rac{Y_l}{|t|^2}$$

Thus tap and phase shift can be represented by the admittance matrix

$$\left[egin{array}{c} ar{I}_1 \ ar{I}_2 \end{array}
ight] = \left[egin{array}{cc} Y_l & -rac{Y_l}{t} \ -rac{Y_l}{t^\star} & rac{Y_l}{|t|^2} \end{array}
ight] \left[egin{array}{c} ar{V}_1 \ ar{V}_2 \end{array}
ight]$$

- if $0 < t \le 1$, this can be represented as a π two-port
- if $0<|t|\leq 1$ but is complex, this is not the case

In the power flow analysis, you must pay attention to this when constructing the system-wide admittance matrix.

Pandapower example

See python notebook / video recording.

References

- Mohan, Ned. Electric power systems: a first course. John Wiley & Sons, 2012.
 Chapter 6.
- Weedy, Birron Mathew, et al. Electric power systems. John Wiley & Sons, 2012. Section 3.8, Section 5.7.
- Course notes of ELEC0014 by Pr. Thierry Van Cutsem.

The end.